

Digital Communications Laboratory

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Chapter Three

Principles of Digital Data Transmission

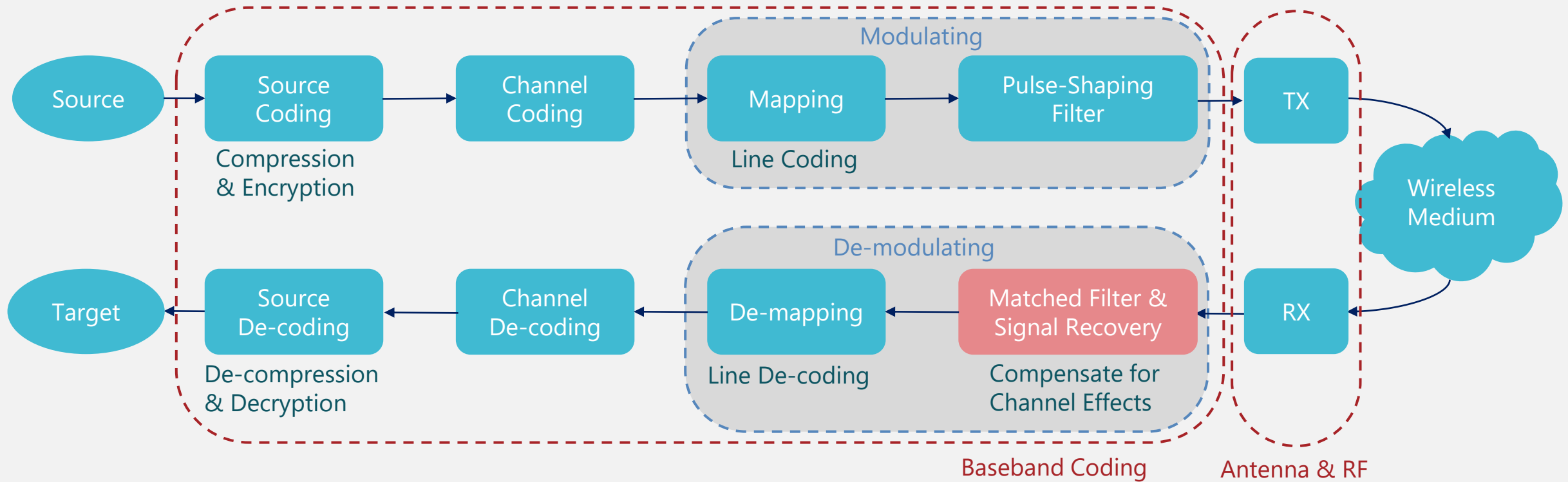


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Section A

Linear Modulation Schemes



Instantaneous Transmitted Signal

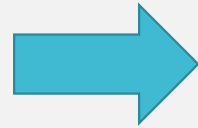
$$S_m(t) = \text{Real}\{A_m g(t) e^{-j(2\pi f_c t + \varphi_m)}\}$$

$$S_{m,BB}(t) = \text{Real}\{A_m g(t) e^{-j\varphi_m}\}$$

A_m : amplitude defined by mapping

φ_m : phase offset defined by mapping

$g(t)$: the pulse-shaping filter



Linear Modulation Types

Linear Modulation	A_m	φ_m	Constellation
ASK/PAM	Variable	Fixed	1D
PSK	Fixed	Variable	2D
QAM	Variable	Variable	2D

Transmitted Data

$$X_m = \sum_{n=0}^{N-1} S_m(t - nT_s) = \text{Real}\left\{ \sum_{n=0}^{N-1} A_m g(t - nT_s) e^{(2\pi f_c(t - nT_s) + \varphi_m)} \right\}$$

Instantaneous Transmitted Signal

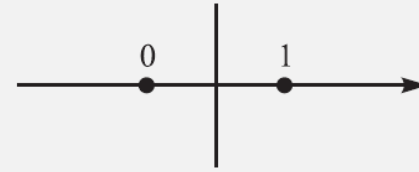
$$S_m(t) = A_m g(t) \cos(2\pi f_c t) = A_m \sqrt{\frac{\epsilon_g}{2}} \varphi(t)$$

M-ary amplitude:

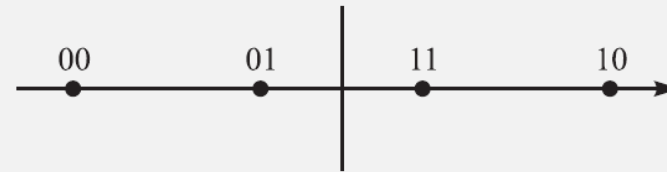
$$A_m = \pm 1, \pm 2, \dots, \pm(M - 1)$$

1D orthogonal basis:

$$\varphi(t) = \sqrt{\frac{2}{\epsilon_g}} g(t) \cos(2\pi f_c t)$$



(a) $M = 2$



(b) $M = 4$



(c) $M = 8$

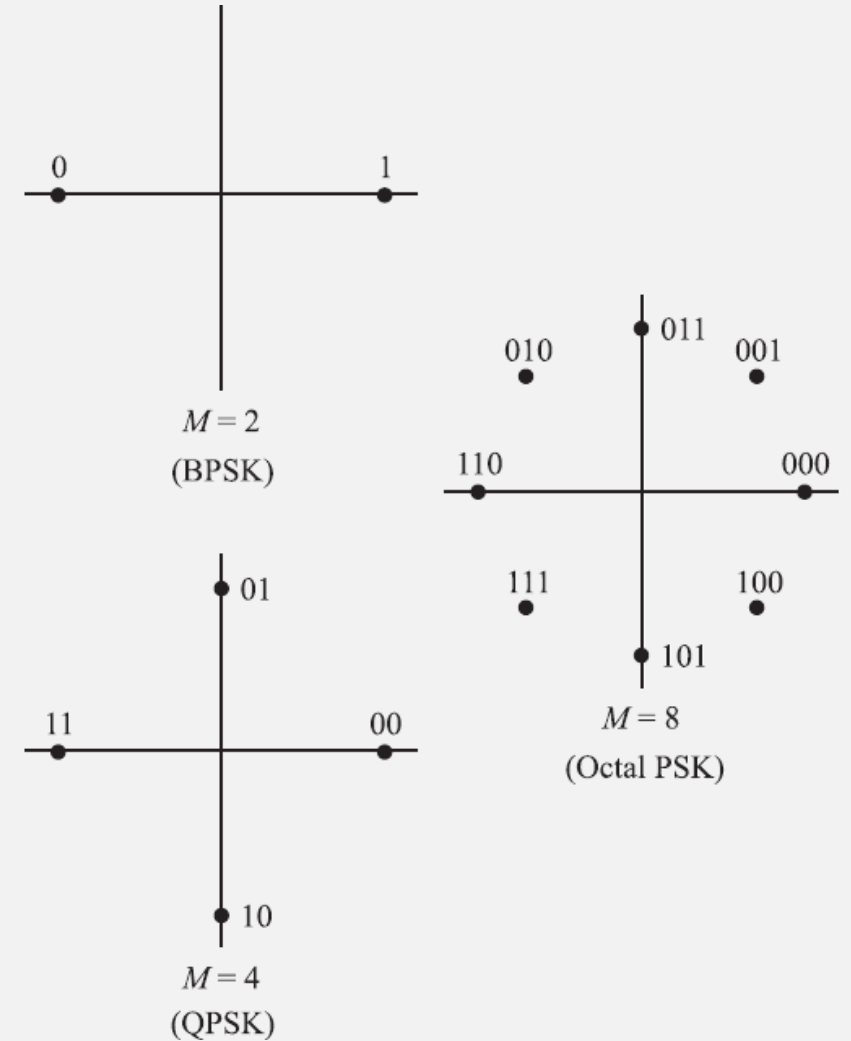
Instantaneous Transmitted Signal

$$S_m(t) = g(t) \cos(2\pi f_c t + \varphi_m)$$
$$= \sqrt{\frac{\varepsilon_g}{2}} \cos\left(\frac{2\pi}{M}(m-1)\right) \varphi_1(t) + \sqrt{\frac{\varepsilon_g}{2}} \sin\left(\frac{2\pi}{M}(m-1)\right) \varphi_2(t)$$

2D orthogonal basis:

$$\varphi_1(t) = \sqrt{\frac{2}{\varepsilon_g}} g(t) \cos(2\pi f_c t)$$

$$\varphi_2(t) = -\sqrt{\frac{2}{\varepsilon_g}} g(t) \sin(2\pi f_c t)$$



Instantaneous Transmitted Signal

$$\begin{aligned} S_m(t) &= A_m g(t) \cos(2\pi f_c t + \varphi_m) \\ &= A_{mi} \sqrt{\frac{\varepsilon_g}{2}} \varphi_1(t) + A_{mq} \sqrt{\frac{\varepsilon_g}{2}} \varphi_2(t) \end{aligned}$$

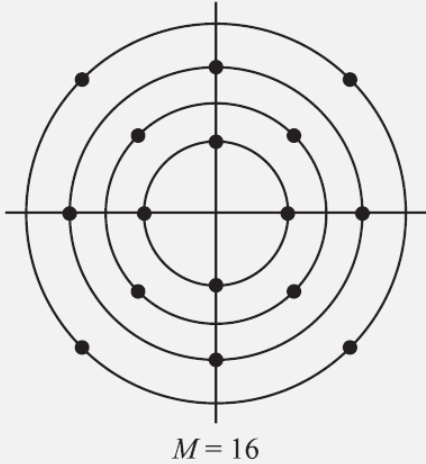
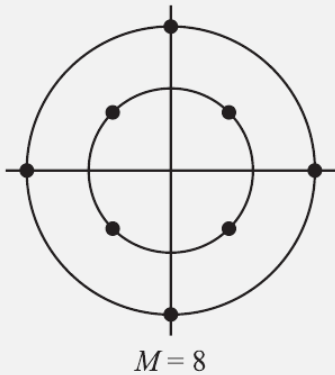
$$A_m = \sqrt{A_{mi}^2 + A_{mq}^2} \quad \varphi_m = \tan^{-1}\left(\frac{A_{mq}}{A_{mi}}\right)$$

2D orthogonal basis:

$$\varphi_1(t) = \sqrt{\frac{2}{\varepsilon_g}} g(t) \cos(2\pi f_c t)$$

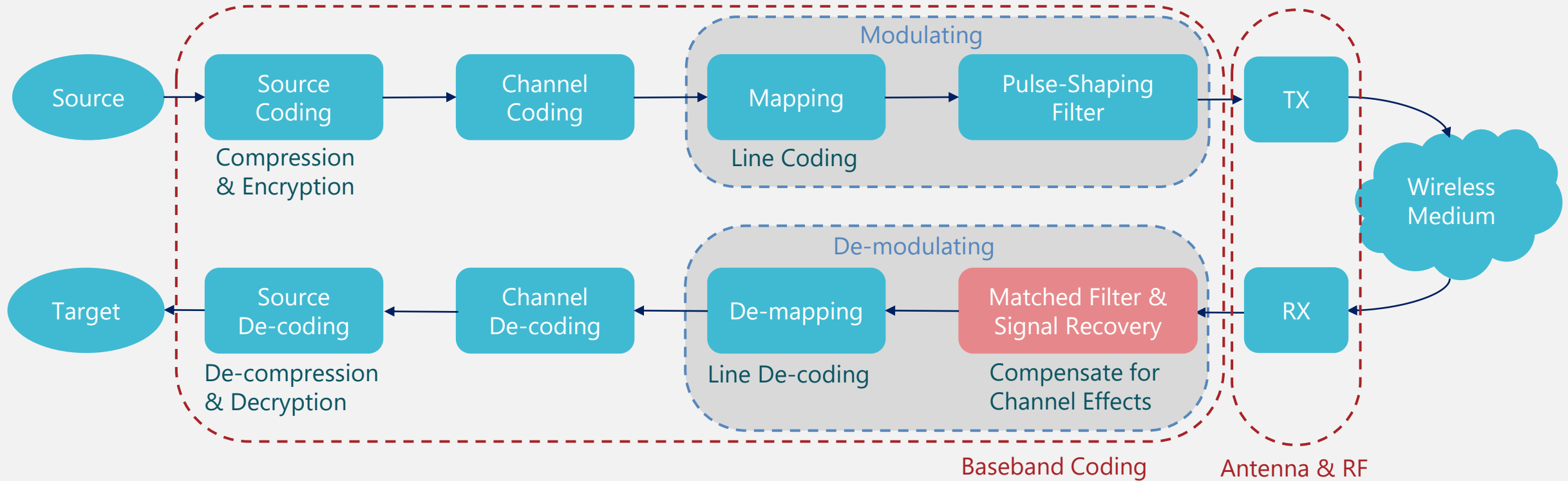
$$\varphi_2(t) = -\sqrt{\frac{2}{\varepsilon_g}} g(t) \sin(2\pi f_c t)$$

$$\begin{aligned} M_{QAM} &= M_{ASK} M_{PSK} \\ K_{QAM} &= K_{ASK} + K_{PSK} \end{aligned}$$



Section B

Non-Linear Modulation Schemes



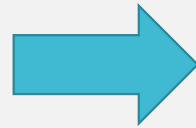
Instantaneous Transmitted Signal

$$S_m(t) = \text{Real}\{S_{m,BB}e^{j2\pi f_c t}\}$$

$$S_{m,BB}(t) = \sqrt{\frac{2\varepsilon}{T}} e^{j2\pi m \Delta f t}$$

$$0 \leq m \leq M \quad 0 \leq t \leq T$$

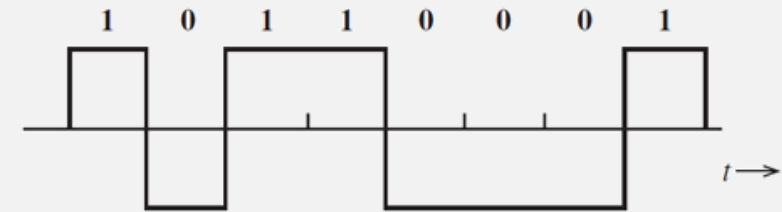
FSK is a special case of the construction of the orthogonal signals.



Non-Linear Modulation Types

Non-Linear Modulation	A_m	φ_m	Constellation
FSK	Fixed	Fixed	MD

Signal



BFSK



Instantaneous Transmitted Signal

$$S_m(t) = \sqrt{\frac{2\epsilon}{T}} \cos(2\pi f_c t + \varphi(t; I) + \varphi_0)$$

$$\varphi(t; I) = 2\pi \sum_{k=-\infty}^n I_k h_k q(t - kT)$$

$$q(t) = \int_0^t g(\tau) d\tau \quad h_k: \text{modulation index}$$

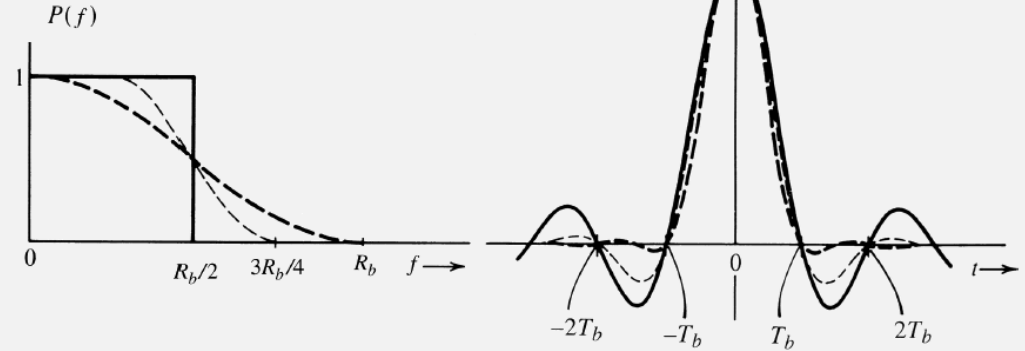
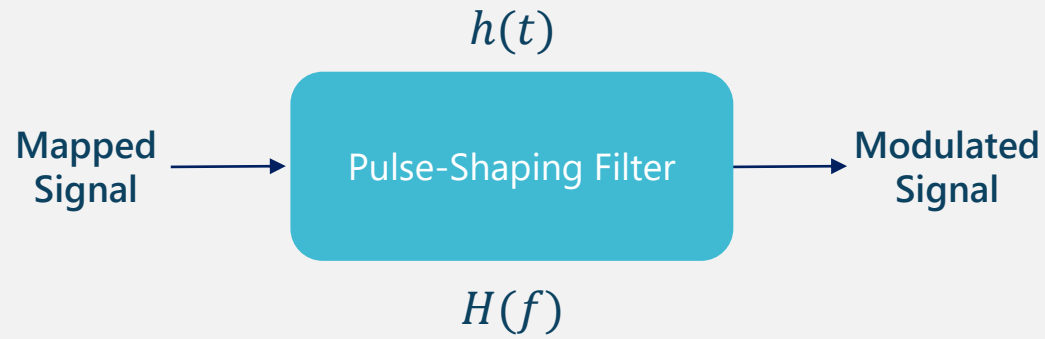
Modulation Types with Memory

Modulation
CPM
CPFSK
MSK
GMSK
OQPSK

- The phase of the signal is constrained to be continuous.
- This constraint results in a phase or frequency modulator that has memory.
- To avoid the use of signals having large spectral side lobes, the information-bearing signal frequency modulates a single carrier whose frequency is changed continuously.

Section C

Pulse-Shaping Filters



Filter Types

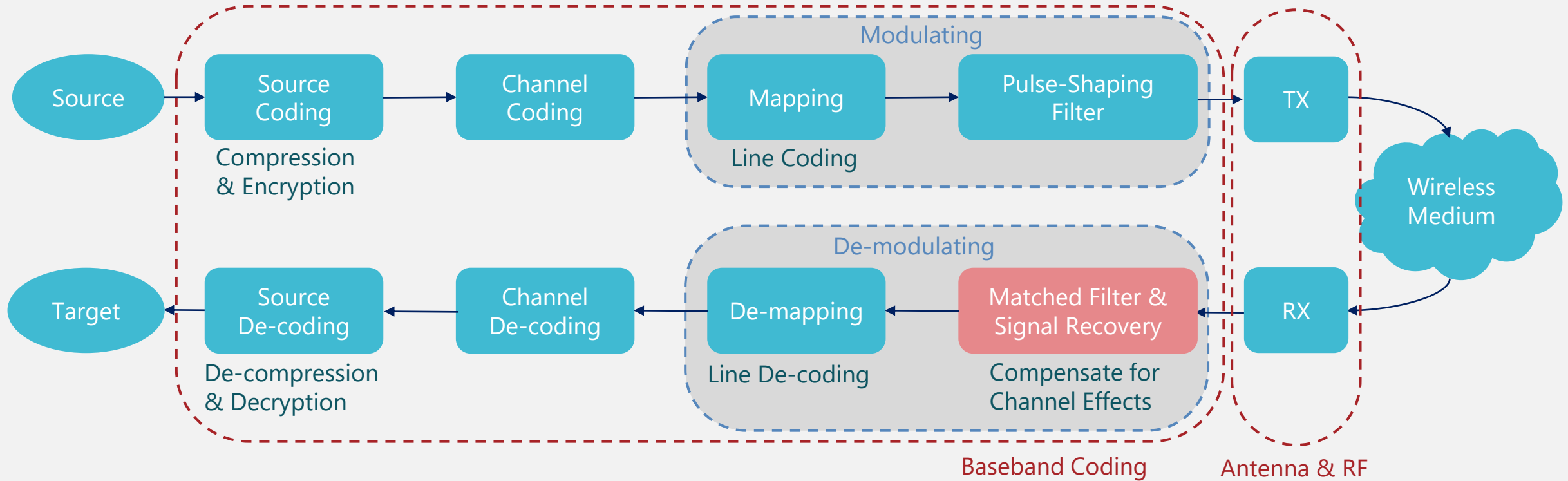
- Rectangular
- Gaussian
- Raised Cosine
- Root-Raised Cosine

Roll-off factor

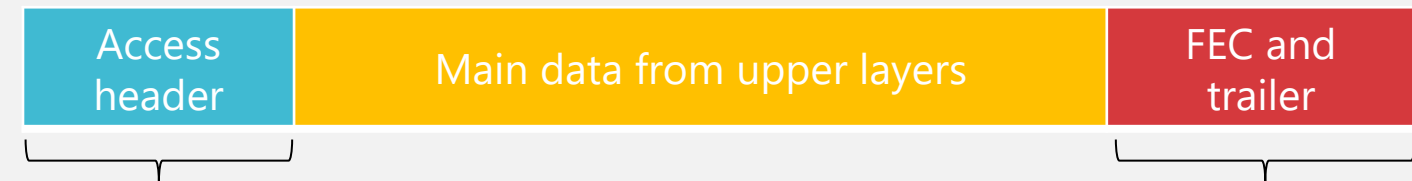
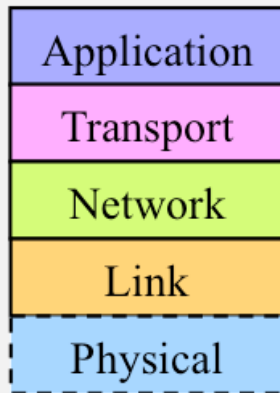
$$h(t) = \begin{cases} \frac{1}{T_s} \left(1 + \beta \left(\frac{4}{\pi} - 1 \right) \right), & t = 0 \\ \frac{\beta}{T_s \sqrt{2}} \left[\left(1 + \frac{2}{\pi} \right) \sin \left(\frac{\pi}{4\beta} \right) + \left(1 - \frac{2}{\pi} \right) \cos \left(\frac{\pi}{4\beta} \right) \right], & t = \pm \frac{T_s}{4\beta} \\ \frac{1}{T_s} \frac{\sin \left[\pi \frac{t}{T_s} (1 - \beta) \right] + 4\beta \frac{t}{T_s} \cos \left[\pi \frac{t}{T_s} (1 + \beta) \right]}{\pi \frac{t}{T_s} \left[1 - \left(4\beta \frac{t}{T_s} \right)^2 \right]}, & \text{otherwise} \end{cases}$$

Section D

Channel Coding/Decoding



Forward error correction (FEC)		Block codes	Linear block codes	Cyclic codes
	Linear block codes	BCH codes	Reed-Solomon codes	-
	Convolutional codes	-	-	-
	Turbo codes	-	-	-
	Space-time coding	Alamouti	Trellis	-



Increases redundancy but simplifies data recovery

Increases redundancy but increases reliability

Section E

GNU Radio and SDR

Preferred GRC Blocks:

Transmitter	Wireless Channel	Receiver
Wav. file source		
Signal source		
Low Pass Filter		
Packet Encoder		
QAM Modulator		
Throttle		
Time sink		
Frequency sink		
Constellation sink		

Note: You may need other essential blocks.